Gottfried Konecny Dietmar Pape Institut für Photogrammetrie und Ingenieurvermessungen Universität Hannover Hannover, Federal Republic of Germany

# Correlation Techniques and Devices\*

The photogrammetric, mathematical, and physical basis of image correlation; the historical development; and recent efforts are reviewed.

#### INTRODUCTION

I MAGE CORRELATION is a procedure of comparing an image, consisting of a two-dimensional sequence of grey-level variations, with a reference image of similar, but not necessarily identical, grey-level variations, in order to detect differences in geometry between these two images. The differences can then be utilized to bring the image into register with the reference image or in order to derive other control signals from them.

In photogrammetry image correlation techniques have been invented and utilized with the main purpose of deriving height information from stereoscopic images in the form of *x*-parallaxes. reference image consists of a given symmetrical signal pattern.

In photogrammetric image correlation the impetus has mainly come from the field of electronic signal processing. The photogrammetrist's interest and influence has mainly been to define the control functions in the photogrammetric evaluation process. The means of achieving the correlation task has been left to the designer of electronic components. He in turn has had reasons or difficulties in communicating his design experiences to the photogrammetrist. The photogrammetrist in turn, began to lose interest as soon as it became evident that electronic image correlation had in-

ABSTRACT: Image correlation techniques are reviewed according to the photogrammetric and mathematical fundamentals as well as the techniques for video-conversion, correlation, and rectification of video signals. The historical development of automatic image correlation devices from the Hobrough Stereomat, via the Bunker Ramo UNAMACE to the Hobrough Gestalt System and the Bendix AS-11-BX is then traced. Reference is made to the Rastar Correlator under development at the University of Hannover, based on designs by G. Hobrough and completed by D. Pape. Finally, other experimental attempts at image correlation, such as (coherent) optical correlation and digital off-line correlation, are summarized.

This was a particularly desirable goal since the measurement of heights by the operator constitutes a considerable human effort, which can then be replaced by an automatic device operating faster with a nearly equivalent performance. Correlators have also been used to measure *y*parallaxes for the purposes of relative orientation. Correlators can also be adapted to the automatic measurement of symmetrical signals for which the

\* Invited Paper, Commission II, 14th Congress of the International Society for Photogrammetry, Hamburg, 13-25 July 1980.

PHOTOGRAMMETRIC ENGINEERING AND REMOTE SENSING, Vol. 47, No. 3, March 1981, pp. 323-333. herent difficulties. For example, heights are measured for areas instead of points, or undesirable information from buildings or trees cannot be eliminated. The photogrammetrist's interest was even more diminished after it became clear that image correlation, despite of its relative speed increase of an order of magnitude, meant a cost increase of not one but two orders of magnitudes for the hardware.

Advantages for automatic correlation could therefore only be demonstrated for very large organizations, i.e., those having a nearly infinite demand for photogrammetric compilation products. For these the use of correlators meant an increase in their production.

The recent electronic design trend toward less expensive components gives rise to new hopes that electronic image correlation may also become economically competitive with fully operatorcontrolled stereo-compilation for the typical photogrammetric plant having a limited product demand.

This process must be viewed under the following aspects: up to now electronic correlators have with few exceptions been designed as total systems. This had made them largely incomprehensible, vulnerable, unserviceable, and most certainly very expensive. On the other hand, analytical plotter development has been generally accepted in photogrammetric instrument design. An analytical plotter possesses a large portion of the components of a photogrammetric image correlation system. It is therefore sufficient to build a correlation device as an added processor to an analytical plotter to have it function as an on-line automatic image correlation system.

Other avenues have been opened by the increased speed, capacity, and flexibility as well as by the decreased cost of computers in general.

Off-line correlation of digitized image information has become feasible. Off-line correlation has the advantage of requiring a minimum of special hardware. On-line correlators, however, have the benefit of refined performance with respect to the quality of measurement and the avoidability of losses because more easily hierarchical decision strategies may be introduced in real time. They also do not have to cope with the large problem of off-line correlation in having to store and address immense quantities of digital data, if a sufficient performance is to be reached.

In this time of changed prerequisites it is quite proper to analyze the past and present achievements in image correlation techniques, but it is even more important to ask the photogrammetric manufacturer and the photogrammetrist in general to become now fully aware of the potential of image correlation in the future.

#### Correlation Techniques for Electronic Correlation

#### PHOTOGRAMMETRIC FUNDAMENTALS

The general task of correlating two images for geometrical differences can be largely simplified if some information about the geometry is known. In this way the known transformation parameters may be applied to both images, and the correlation task becomes restricted to those parameters which are not predeterminable.

In aerial photography an image point x'y' is related to a ground point X,Y,Z by the collinearity equations, i.e.,

$$\begin{aligned} x' &= x_c' - c \\ &= \frac{a_{11}(X - X_0) + a_{12}(Y - Y_0) + a_{13}(Z - Z_0)}{a_{31}(X - X_0) + a_{32}(Y - Y_0) + a_{33}(Z - Z_0)} + \frac{\Delta x'}{(1)} \\ y' &= y_c' - c \\ &= \frac{a_{21}(X - X_0) + a_{22}(Y - Y_0) + a_{23}(Z - Z_0)}{a_{31}(X - X_0) + a_{32}(Y - Y_0) + a_{33}(Z - Z_0)} + \frac{\Delta y'}{(1)} \end{aligned}$$

The collinearity equations include

- (1) the three known parameters of interior orientation  $x'_c$ ,  $y'_c$ , and c;
- (2) the exterior orientation parameters: of these  $X_0, Y_0, Z_0$  are the three exposure station coordinates in the ground system. The nine coefficients  $a_{11}$  to  $a_{33}$  are functions of the three camera rotations  $\omega, \phi, \kappa$  with respect to the ground coordinate system, defined by a rotational matrix. Relative orientation of one image with respect to the other, in which the image is reprojected to the reference image to coincide in five different points permitting only z-variations, determines five of the exterior orientation parameters; and
- (3) the image displacements  $\Delta x'$ ,  $\Delta y'$  caused by distortion of various kinds such as
  - (a) lens distortion as function of x'y',
  - (b) film deformation as function of x'y',
  - (c) refraction as function of exterior orientation, and
  - (d) coordinate system deformation (deviations from orthogonality of the ground coordinate system).

Photogrammetric restitution instruments are capable of compensating with plotting accuracy for most, if not all, of these deformations.

Photogrammetric cameras operate nearly lensdistortion free and the deformations of film, refraction, and the ground coordinate system are generally negligible in plotting. Analog plotters use optical or mechanical projection of the images by making use of the known or otherwise determined or assumed three interior and six exterior orientation parameters of each photograph. Analytical plotters establish the relations by a digital solution of the collinearity equations.

But plotters only solve the relationship for one point. The point setting includes stereoscopic measurements by the operator involving a correlation process in his brain. Automatic image correlation techniques therefore must be applied to a two-dimensional sequence of points. This is principally possible in the following ways:

• The images are projected by the collinearity equations onto a rectified image plane which serves as a basis for correlation. The first Hobrough Stereomat operated on images projected onto the platen of a Kelsh plotter in this manner.

324

Also, the IBM-DAMCS rectified the image before digital correlation. This "model space correlation" has the advantage of an optimal correlation geometry. It has the disadvantage, however, of grey level losses during the analog projection or of tedious resampling operations in digital projection.

- It is possible to select model spaces other than reprojection onto a rectified image plane. Such a possibility is the selection of a sequence of corresponding epipolar lines in the two images. An epipolar line is the trace (intersection) of the model plane defined by a ground point and the two exposure stations in the plane of the photograph. Calculation of the corresponding epipolar lines involves selection of a ground point, calculation of the two corresponding image points, x'y'and x''y'', by collinearity equations, and the calculation of the directions of the epipolar lines. dy'/dx' and dy''/dx'', by explicit or implicit means. Epipolar correlation, first applied by Helava in the AS-11B-X, reduces the problem of transforming thousands of image points by projection. Instead, it restricts itself to the projection and correlation of only hundreds of points along an epipolar line. This is possible by a moderate digital computation effort in real time.
- "Brute-force" image correlation utilizes area sensors which may or may not have been positioned to corresponding points, x'y' and x''y''. Such correlation uses input images which have not yet been geometrically transformed. The geometric transformations for correlation can be achieved during the correlation process in two ways:
  - Either at first no transformation at all is applied and subsequent transformation parameters are calculated from a first rough correlation and the process is iteratively improved;
  - or a sampling algorithm operating according to the collinearity equations is applied in order to select a specific sequence of image points. Such a procedure can generally operate fast enough only when electronic circuitry combined with flying spot scanner sampling is applied. Such a procedure may also be useful in off-line digital correlation.

Image correlation has as its aim the registration of images or transformed images. While the described displacements caused by parameters of interior and exterior orientation, including the various distortion types, affect image portions, individual height displacements,  $\Delta z$ , are those which vary most in the model and which are detectable in the projected images as x-parallaxes, as parallaxes along the epipolar line in an epipolar system, or as terrain samples obtained by the brute force correlator.

To detect these variations in  $\Delta z$  as a function of x,  $x_{epipolar}$ , or as some other function of x'y', a limited window must be defined in which correlation in two or at least in one dimension is performed in order to define z from a selected number of points characteristic for this limited sample (see Figure

1). It is possible to treat the sampled information referring to a region in such a way as to favor its mean or its center and, even, to derive z as function of the sampled sequence. In this respect the width of the correlation window assumes an important role.

Image correlation is also influenced by photometric distortions resulting from different viewing angles, which cause different reflection characteristics affecting in general the low frequency component of the grey level sequences but also high frequency details (see Figure 2).

#### MATHEMATICAL FUNDAMENTALS

For the determination of a best match for two corresponding one-dimensional signal sequences (original or transformed), a correlation algorithm must be used.

If A(t) is the sequence of grey level signals contained in the reference photo and  $B(t + \tau)$  the sequence of grey level signals contained in the photo to be shifted, the shift being characterized by  $\tau$  in the signal sequence, then the correlation integral,  $R(\tau)$ , valid for the correlation window, -Tto +T, is given by

$$R(\tau) = \frac{1}{2T} \int_{-T}^{T} (A(t) \cdot B(t + \tau) dt.$$
 (2)

The correlation integral can be calculated for a sequence of signals A(t) and  $B(t + \tau)$  chosen arbitrarily.

Then one of the signals is shifted by  $\Delta_i$  (and by negative and positive multiples thereof) and the  $R(\tau + \Delta_i)$  are again calculated, i.e.,

$$R(\tau + \Delta \tau_i) = \frac{1}{2T} \int_{-T}^{T} (A(t) \cdot B(t + \tau + \Delta \tau_i) dt . (3))$$

One of the values calculated for  $R(\tau + \Delta \tau_i)$  will become a maximum, and this  $\Delta \tau_i$  will be the required optimal shift.  $\Delta \tau_i$  is directly proportional to the required change in  $\Delta z$ .

The correlation integral to be maximized may be

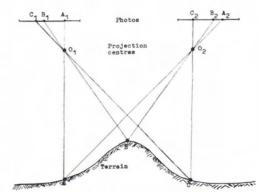


FIG. 1. Geometric distortion due to terrain elevations.

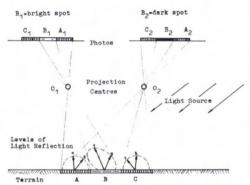


FIG. 2. Photometric distortion caused by different reflections in different viewing angles.

replaced by other functions of identical or at least similar effect, e.g.,

• The correlation integral expressed as a finite correlation coefficient, i.e.,

$$r(\Delta \tau) = \frac{\sum A(t) \cdot B(t + \Delta \tau)}{\sum (A(t))^2 \cdot (A(t + \Delta \tau)^2)}, \qquad (4)$$

this coefficient to be maximized;

- The covariance of the two signals, to be maximized;
- The square sum of the residuals, to be minimized;
- The absolute difference of the residuals, to be minimized;
- The cross correlation of the Fourier spectra of the two images, to be maximized; or
- The correlation intensity, I, to be maximized, i.e.,

$$I(\Delta \tau) = \sqrt{\Sigma |A(t)|^2 + \Sigma |B(t + \Delta \tau)|^2}.$$
 (5)

The optimal determination of  $\Delta \tau$  in the two directions,  $\Delta x$  (or  $\Delta x'$ ) and  $\Delta y$  (or  $\Delta y'$ ), becomes a function of the grey level distribution and its disturbances. It is possible to optimize its determination by the proper choice of filtering operations. Since it is desired to reduce the number of required computations, the difference of the chosen correlation algorithm function can be selected as a measure to control the computation process; i.e.,

$$\Delta R(\tau) = R_1(\tau) - R_2(\tau) \tag{6}$$

where

$$R_{1}(\tau) = \frac{1}{2T} \int_{-\tau}^{\tau} A(t + \Delta \tau) \cdot B(t + \tau) dt \text{ and} \quad (7)$$

$$R_{2}(\tau) = \frac{1}{2T} \int_{-\tau}^{\tau} A(t) \cdot B(t + \tau + \Delta \tau) dt.$$
 (8)

Likewise, algorithms other than the correlation integral are applicable.  $\Delta R(\tau)$  permits the control and convergence of the image correlation process toward a state of maximization of the correlation integral (correlation coefficient) or the minimization of the parallax difference (square sum of residuals).

 $\Delta R(\tau)$  to be minimized may also be obtained by differentiating the signal  $R(\tau)$  to be maximized.

### VIDEO CONVERSION

In the photographs the total image information is available simultaneously (in parallel). To make this information electronically accessible, it must be converted into a serial sequence of electric signals. For this purpose the photographs are quantized into their smallest image elements and these are sequentially or in groups transmitted to electro-optical sensors. Sensors to convert density differences of images into electric currents conventionally have been photo-cathodes or solid state sensors. Photo cathodes embrace photo-cells, photo-multipliers, and vidicons; solid state sensors resemble photodiodes, especially those combined into arrays. In order to permit a sequential scanning, the image elements are either simultaneously imaged onto a group of sensor elements, which are serially interrogated element by element (vidicon, diode-arrays) or which are serially illuminated and imaged by a single photo sensor (flying spot CRT, laser, Nipkow-disk). In modifying and processing of the analog signals nonpredictable disturbances may be generated by thermal noise and by foreign sources. In this respect the flying spot Laser and the photodiode array have proven to be very useful. After digitization of the signals, these error influences disappear almost completely, so that an early A/D conversion is considered desirable in the course of signal processing.

#### CORRELATION OF VIDEO SIGNALS

Correlation of the two video signals derived from both stereo images may be analog or digital. The digital procedure has its advantages. The functions to be performed are delay, multiplication, integration, and subtraction. Furthermore, filtering operations are most essential in order to diminish the sensibility to obtain side-maxima of the correlation integral. Figure 3 describes the realization of a correlator based on Equation 3. Figure 4 describes the realization of a correlator based on Equation 6.

By the choice of suitable frequency bands of the filters and by suitable choices for  $\Delta \tau$ , the parallax can be determined in several steps beginning with the large area image content going on to the finest image details.

#### **RECTIFICATION OF VIDEO SIGNALS**

Even if there are no correction possibilities for the photometric differences of the two images to be correlated, the geometric distortions, particularly those due to elevation differences, may be

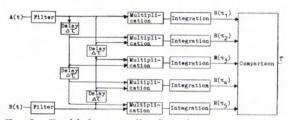


FIG. 3. Establishing parallax from the maximum correlation function.

determined and corrected well. For this purpose both photos are controlled in an independent manner. One possibility for rectification exists as follows:

A number of image elements, sufficient to cover the range of the maximum expected parallax, is stored electronically. In this case rectification can occur later digitally. The advantage of this procedure is that rectification is independent of image scanning performed before. Therefore, image scanning may be greatly simplified using a regular scanning mode. The control of the rectification process occurs during correlation from parallax values obtained.

Another possibility for rectification exists in controlling the sampling speed or direction of scan. In this case the hardware effort is considerably larger.

Figure 5 shows the principle of a correlator with electronic rectification. With appropriate scaling the rectification may correspond to information contained in an orthophoto. The output may not only be in form of parallaxes, but also directly as *z* values.

#### **ELECTRONIC CORRELATION DEVICES**

#### ELECTRONIC ANALOG CORRELATION

The history of electronic correlation is depicted in Table 1. The first historical developments concern electronic analog correlation devices. Only the more recent correlation devices contain digital elements.

#### ELECTRONIC DIGITAL CORRELATION

The Bendix AS-11B-X, the Gestalt Photomappers, and the Jenoptik Oromat already contain such digital correlation elements. But in particular the Rastar-Correlator, developed at the Institut für

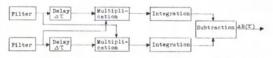


FIG. 4. Establishing the slope of the correlation function for subsequent parallax elimination.

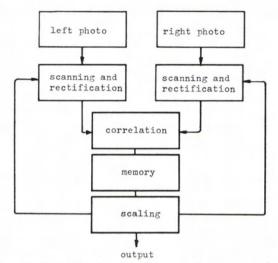


FIG. 5. Principle of a correlator with electronic rectification.

Photogrammetrie und Ingenieurvermessungen of the Universität Hannover since 1976, is a fully digital correlation system. After a simultaneous exposure of 1728 image elements with an exposure time of 2 ms, the electric charges corresponding to the exposures are transferred to a CCD and transmitted in series digitally to memory. CCD-chips are linear arrays located on rotable servo-controlled mounts. In this way the diodearrays may be turned into the epipolar direction, which is continuously calculated from image coordinates in the restitution computer.

A certain photometric correction of the signals is performed partially before and partially after digitization. In particular, this concerns errors due to deviations in transfer characteristics of the different photo-diodes of an array and contrast enhancement in photo areas of high density with logarithmic transfer.

Rectification, filtering, correlation, and composition of parallaxes obtained by various frequency bands is performed in various digital circuits designed for the purpose to derive a parallax curve over the extent of the 12 mm photo-line-width. Universal circuits can only be used infrequently, because of the high speed requirement necessitating 200 computer operations per  $\mu$ s to conclude a correlation computation for an epipolar line combination in 2 ms. The special circuits can be housed in a 19-inch cabinet of 2 height units (88 mm).

The development of the Rastar-Correlator was brought to a first conclusion with a functional demonstration in 1979. Presently, further modifications and improvements to adapt it for various applications are being made (see Figure 6).

year	device name	manufacturer	photo- sensing	rectification within the correlation window	filtering	size of correlation window	method of parallax detection
1958	Stereomat I	Photographic Survey Corp., Toronto, G. L. Hobrough	flying spot random scan	none	analog		
1962	Automatic Map Compilation System	Ramo- Woolridge		none		$\begin{array}{c} 1,27\times1,27\\ \mathrm{mm}^2 \ \mathrm{to}\\ 5,08\times5,08\\ \mathrm{mm}^2\end{array}$	
1962	Automatic Stereo Mapping System	Ramo- Woolbridge (Bunker Ramo)	Nipkow- disc	mechanically linear			orthogonal cross corre- lation analog
1963	Stereomat III (II?)	Hunting Sur- vey Corp., Toronto, G. L. Hobrough	flying spot epipolar lines	analog linear	analog		
1963	Projection Stereo Plotter AP-14	Librascope Div/Gen. Precision Inc.	flying spot rosette	linear		automatic- ally con- trolled by terrain slope	
1964	Stereomat IV	Benson- Lehner	flying spot	linear analog	analog	variable with auto- matic control by correlation quality	maximum of cross corre- lation
1966	Universal Automatic Map Compi- lation Equipment (UNAMACE)	Ramo-Wool- ridge	TV-raster 128 lines		7 octav bands		

TABLE 1. EVOLUTION OF ON-LINE CORRELATORS FOR AUTOMATION IN PHOTOGRAMMETRY

328

# PHOTOGRAMMETRIC ENGINEERING & REMOTE SENSING, 1981

1966	AS-11-B AS-11-C	Bendix	flying spot random scan			automat- ically controlled by corre- lation function	orthogonal cross corre- lation, dig- ital
1968	Stereomat A 2000	Raytheon Automatic	flying spot random scan				
.968/70	ITEK EC-5	ITEK	flying spot diagon. raster		several bands analog		
1970	Gestalt Photomapper	G. L. Hobrough	flying spot in epi- polar lines TV-raster 8 × 9 mm	high degree	6 octav bands	inversely propor- tional to degree of rectifi- cation	orthogonal cross corre- lation
	OroMAT	Jenoptik	flying spot, deformed TV-raster	longitudi- nal and lateral tilt	3 frequen- cy bands, analog	$\begin{array}{c} 3 \text{ raster} \\ \text{sizes} \\ 4 \times 4 \text{ mm} \\ 3 \times 2 \text{ mm} \\ 2 \times 1 \text{ mm} \end{array}$	orthogonal cross corre- lation, digital
1978	AS-11B-x	Bendix	Laser with rotating prisms, epipolar lines	polygon with maxi- mal 58 corners, digital	digital	3 sizes	
1980	Rastar	Hobrough/ IPI-Hannover	linear photo- diode arrays, epipolar lines	polygon with 256 corners, digital	7 octav bands, digital	0,08 5,4 mm	maximum of correlation function

-

## PHOTOGRAMMETRIC ENGINEERING & REMOTE SENSING, 1981

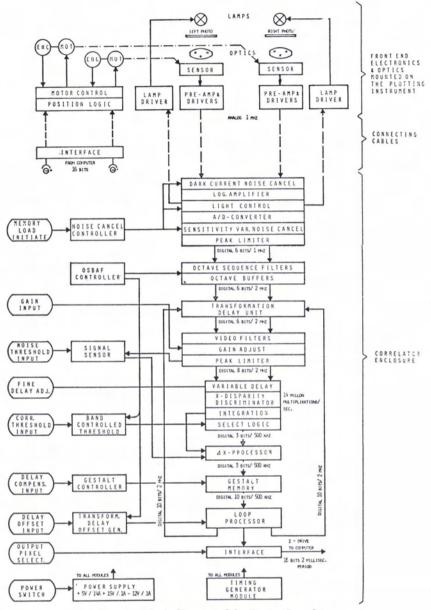


FIG. 6. Block diagram of the Rastar Correlator.

#### OTHER EXPERIMENTAL ATTEMPTS FOR IMAGE CORRELATION

#### OPTICAL CORRELATION

The fact that image correlation may also be achieved by maximal cross-correlation of the Fourier-spectra of two images has been demonstrated by coherent optical procedures which can easily generate a Fourier spectrum directing a laser beam through image portion.

Krulikoski of the Bendix Corp. demonstrated the

first success generating elevation profiles by optical correlation.

Balasubramanian was able to build a coherent optical correlator, based on optical correlation principles using heterodyne techniques.

Inherent to optical correlation is a relatively easy parallel access to frequency information. A handicap, however, is the limited control capability during the evaluation process. In particular, rectification within the correlation window is not possible. For that reason optical correlators do not

# CORRELATION TECHNIQUES AND DEVICES

year	name	realized by	input	correlation algorithm	remarks
1964	DAMCS	Sharp et al., IBM	resampled rectified digitized photograph	correlation coefficient maximized	demonstration of orthophoto and contour output
1974	UCL-System	Dowman	scanned in epipolar lines on CP1-AP/C digitized photo	cross-co- variance correlation coefficient, error function, square err. function, quotient err. function.	experimental, less expensive, and less sophisti- cated method
1974	DIMES	Gambino <i>et al.</i>	raster scan digitized photo	peak of corre- lation func- tion, 2-dimensional	array processor for handling high speed de- mands
1974	UNB-System	Masry	scanned in epipolar lines digitized photo	"an algorithm"	experimental
1975		Keating et al. (Univ. of Maine)	close to flight line scanned raster digi- tized photo	euclidean difference, normalized encl. diff., norm. cross correlation coeff., Hada- mard trans- formation	2-dimensional for orientation, 1-dimensional for final scan
1976		Kreiling	raster scanned digitized photo		
1977		Göpfert	raster scanned digitized photo	peak of: autocorrel. coeff., cross " ", auto " intensity, cross " "	comparison for best correlation results of al- gorithms
1978		Konecny et al.	Scanned in epi- polar lines (by prepro- cessor) digi- tized photo	peak of cross correlation coefficient	suggested experi- mental system
1978		Girard (Etablisse- ment Tech- nique Central de l'Arme-	resampled rec- tified digi- tized photo	peak of cross correlation coeff. no geometric	experimental
		ment Arcueil, France)		rectification in correla- tion window	
1978		Panton, CDC	raster scan oriented to flight direc- tion digitized photo	peak of corre- lation func- tion	demonstration of contour, 3 D, and rectified grid output
1979		Macarovic	arguizea photo		in preparation for ISP Congress 198

TABLE 2. DIGITAL OFF-LINE CORRELATION

PHOTOGRAMMETRIC ENGINEERING & REMOTE SENSING, 1981

reach the performance required for height measurements.

#### DIGITAL OFF-LINE CORRELATION

Table 2 summarizes the past digital attempts to correlate image information which has been scanned and stored. As can be seen from the table, most attempts have been made in the last few years. The reason for this may be the increased computer capability in speed and storage. But still off-line correlation seems to be much too expensive for utilization in medium sized photogrammetric plants, particularly if there is a need for specialized computer systems with very fast processors for off-line correlation. Because the costs of fast standard computer time and of memory size are still rapidly going down in contrary to the cost of specialized hardware, off-line correlation may eventually in the near or far future become competitive to on-line correlation with respect to comparable accuracy and reliability requirements. This will happen when mass storage becomes inexpensive enough to store the total information from the photos; or it may happen when methods of preprocessing are developed which scan the photo information selectively in the manner of an operator who assists an on-line correlation system coming into trouble for some reason.

## CONCLUSIONS

Looking at the reviewed correlation techniques and devices, the following general conclusions can be made:

- Image correlation becomes more and more feasible in photogrammetry,
- In the near future on-line correlation will dominate over off-line correlation in photogrammetric production, and
- Attempts in evaluating off-line correlation systems are made with increasing effort. Economic application in photogrammetry depends on progress in computer developments.

#### BIBLIOGRAPHY

- Balasubramanian, 1974. Image Coincidence Detection using Optical Correlation Techniques. *Coherent Optics in Mapping*, Proc. of the Soc. of Photo-Optical Instr. Eng., Vol. 45, pp. 221-228.
- Bertram S., 1962. Automatic Map Compilation. Photo. Eng., Vol. 28, pp. 184-188.
  - —, 1963. The Automatic Map Compilation System. Photo. Eng., Vol. 29, pp. 657-679.
  - —, 1965. The Universal Automatic Map Compilation Equipment. *Photo. Eng.*, Vol. 31, pp. 244-260.
  - —, no date. The Universal Automatic Map Compilation Equipment. Bunker Ramo Corporation, Brochures.
- Birnbaum, M., and P. M. Salomon, 1964. A High Speed, Inertia-Free Automatic Stereoplotting Instrument. *Photo. Eng.*, Vol. 30, pp. 842-852.

- Blachut, T. J., and U. V. Helava, 1960. Automatic Stereo Plotting in Small and Large Scale Mapping, Bericht zum 9. Internationalen Kongreß für Photogrammetrie, London.
- Boyajean, J., 1961. The Implementation of the Integrated Mapping System. *Photo. Eng.*, Vol. 27, pp. 55-60.
- Brucklacher, W., 1968. Automatische Orthoprojektorsteuerung durch Planimal mit Korrelator. Bildmessung und Luftbildwesen, Vol. 35, pp. 117-120.
- Chappelle, W. E., 1964. Automated Analytical Stereoplotter Design Data and Analysis. Rome Air Development Center, U.S. Air Force Project No. 5569.
- Cude, W. C., 1960. Automatic and Semiautomatic Mapping. *Photo. Eng.*, Vol. 26, pp. 303-306.
- Deker, H., 1962. Prebleme und Erfolge der Automation in der Photogrammetrie. Bildmessung und Luftbildwesen, Vol 30.
- Dowman, I. J., 1977. Developments in On-line Techniques for Photogrammetry and Digital Mapping. *Photo. Rec.*, Vol. 9(49), pp. 41-54.
- Dowman, I. J., and A. Haggag, 1977. Digital Image Correlation along Epipolar Lines. Proc. of the Int. Symp. on Image Processing, Graz, pp. 47-49.
- Drum, D. E., and G. M. Elphingstone, 1978. Experience with the AS-11B-X Epipolar Plotter. ISP Paris, pp. 200-214.
- Esten, R. D., 1957. Automatic Contouring. *Photo. Eng.*, Vol. 23, pp. 49-53.
- -------, 1964. Automatic Photogrammetric Instruments. Photo. Eng., Vol. 30, pp. 544-558.
- Forrest, R. B., W. H. Moore, and F. A. Scarano, 1968. Automatic Comparator. *Bendix Technical Journal*, Vol. 1, No. 2, pp. 76-80.
- Gambino, L. A., and M. A. Crombie, 1974. Digital Mapping and Digital Image Processing. *Photo. Eng.*, Vol. 40, pp. 1295-1302.
- Girard, M., 1978. Correlation Automatique des Photographies Stereoscopiques. Equipment for Analytic Photogrammetry and Rem. Sens., ISP Paris, pp. 406-415.
- Göpfert, W. M., 1977. Digital Cross Correlation of Complex Exponiated Inputs. Proc. of the Int. Symp. on Image Processing, Graz, pp. 63-66.
- —, 1978. Digitale Korrelation komplex exponierter Daten. Z.f.V. 10/1978, pp. 475-484.
- De Graaf, R. M., 1964. Automation Characteristics of the Stereomat B8. *Photo. Eng.*, Vol. 30, pp. 818-824.
- Hardy, J. W., H. R. Johnston, and J. M. Godfrey, 1968. An Electronic Correlator for the Planimat. Intern. Archiv für Photogrammetrie, Lausanne, Kommission II.
- —, 1970. Automatic Stereoplotting with the EC-5/ Planimat. Bildmessung und Luftbildwesen, Vol 38., pp. 62-68.
- Helava, U. V., 1957. New Principle for Photogrammetric Plotters. *Photogrammetria*, pp. 89-96.
  - —, 1964. Some Thoughts on Automation in Photogrammetry. *The Canadian Surveyor*, Vol. 18.
- —, 1976. Digital Correlation in Photogrammetric Instruments. ISP Helsinki.

—, 1978. The AS-11B-X Image Correlation System. Symp. Eins. dig. Komp. Phot., Hannover.

- Helava, U. V., and W. E. Chappelle, 1972. Epipolar-Scan correlation. *Bendix Technical Journal*, Vol. 5, No. 1, pp. 19-23.
- Helava, U. V., and R. H. Seymour, 1976. US-1 Universal Stereoplotter. ISP Helsinki.
- Helava, U. V., A. E. Whiteside, und C. W. Matherly, 1968. New Automatic Analytical Stereoplotter. Bendix Technical Journal, Vol. 1, No. 2, pp. 72-75.
- Hobrough, G. L., 1959. Automatic Stereo Plotting. Phot. Eng., Vol. 25, pp. 763-769.
  - -----, 1960. Automatic Stereo. ISP London.
  - —, 1965. Automation in Photogrammetric Instruments. *Photo. Eng.*, Vol. 31, pp. 595-603.
  - —, 1978. Digital On-Line Correlation. Symp. dig. Kompon., Hannover.
- Hobrough, G. L., and J. M. Ham, 1961. The Control System of an Automatic Stereomapping Machine. *Transactions the Engineering Institute of Canada*, No. 3.
- Hobrough, G. L., and T. B. Hobrough, 1970. Image Correlator Speed Limits. ISP Com. II, München.
- Hobrough, G. L., and G. A. Wood, 1964. Automatic Image Registration. International Archive for Photogrammetry, 10. Intern. Congress, Lisbon.
- Johnson, E. C., and A. Di Pentima, 1964. Image Correlation System for Analytical Stereoplotters. International Archive for Photogrammetry, 10. Internat. Congress, Lisbon.
- Kamm, V. C., A. J. Foland, R. R. van Andel, L. W. Behr, and R. E. Childs, 1968. Design of the Bx-272 Integrated-Circuit Control Computer. *Bendix Technical Journal*, Vol. 1, No. 2, pp. 14-20.
- Keating, T. J., and P. R. Wolf, 1976. Analytical Photogrammetry from Digitized Image Densities. ISP Helsinki.
- Keating, T. J., P. R. Wolf, and F. L. Scarpace, 1975. An Improved Method of Digital Image Correlation. *Photo. Eng. and Rem. Sens.*, Vol. 41, pp. 993-1002.
- Kelly, R. E., P. R. H. McConnell, and S. J. Mildenberger, 1977. The Gestalt Photomapping System. *Phot. Eng. and Rem. Sens.*, Vol. 43, pp. 1407-1417.
- Konecny, G., 1978. Development and Possibilities of Digital Image Correlation and Digital Differential Rectification. Equipment for Analytic Photogrammetry and Rem. Sens., ISP Paris, pp. 387-405.
- Konecny, G., H. Kazmierczak, and P. Gemmar, 1978. Digitale Prozessoren für Differentialentzerrung und Bildkorrelation. *BuL*, 3/1978, pp. 99-109.
- Kosofsky, L. J., and C. S. Spooner, 1964. An Integrated Mapping System. Photo. Eng., Vol. 26, pp. 131-135.
- Kreiling, W., 1976a. Automatische Herstellung von Höhenmodellen und Orthophotos aus Stereobildern durch digitale Korrelation. Diss. Univ. Karlsruhe.
  - —, 1976b. Automatische Auswertung von Stereobildern durch digitale Korrelation. ISP Helsinki.
  - —, 1978. Off-Line Image Correlation in General Purpose Computers. Symp. über den Einsatz dig-

italer Komponenten in der Photogrammetrie. IPI Hannover Feb. 1978.

- Leighty, R. D., 1974. Coherent Optics Potential to Mapping. Coherent Optics in Mapping, Proc. of the Soc. of Photo Optical Instr. Eng. Vol. 45, pp. 113-130 (Rochester, N.Y.)
- Lindig, G., 1976. Weitere Erfahrungen mit dem ITEK-Korrelator EC 5 ISP Helsinki 1976, Komm. II.
- Löscher, W. 1964. The B8-Stereomat. Photogrammetric Record 1964, pp. 476-482.
- Makarovic, B., and K. Tempfli, 1979. Digitizing Images for Automatic Processing in Photogrammetry. *ITC-Journal* 1979-1, pp. 107-126.
- Marckwart, W., 1976. The Production of Stereo-Orthophotos with the Topocart-Orthophot C Instrument System of VEB Carl Zeiss Jena. ISP Helsinki 1976, Comm. II.
- —, 1979. Application and accuracy of the Topomat automatic restitution system. Kompendium Photogrammetrie VO. XIII, Leipzig 1979, pp. 121-129.
- Masry, E., 1974. Digital Correlation Principles. Phot. Eng., Vol. 40, pp. 303-308.
- Masry, E., B. G. Crawley, and W. H. Hilborn, 1975. Difference Detection. *Phot. Eng. and Rem. Sens.*, Vol. 41, pp. 1145-1148.
- De Meter, E. R., 1963. Latest Advances in Automatic Mapping. Phot. Eng., Vol. 29, pp. 1027-1036.
- Nims, D. J., 1974. Optical Correlators—Moving Beyond the Breadboard. *Coherent Optics in Mapping*, Proc. of the Soc. of Photo-Optical Instr. Eng. Vol. 45, pp. 215-220.
- Pryor, W. T., and J. H. Watson, 1966. Ominstereomeasurer BRP. *Phot. Eng.*, Vol. 32, pp. 830-832.
- Panton, D. L., 1978. A Flexible Approach to Digital Stereo Mapping Phot. Eng. and Rem. Sens., Vol. 44, pp. 1499-1512.
- Pape, D., 1978. Hardware Implementierung eines digitalen Bildkorrelators. Sympos. über d. Einsatz dig. Komp. i.d. Photogrammetrie, IPI Hannover.
- Sharp, J. V., R. L. Christensen, W. L. Gilman, and F. D. Schulmann, 1965. Automatic Map Compilation Using Digital Techniques. *Photo. Eng.*, Vol. 31, pp. 223.
- Schwidefky, K., 1963. Die Grenzen von Mensch und Automat in der Photogrammetrie, Vermessungstechnik.
- Spooner, C. S., Jr., S. W. Dossi, and M. G. Misulia, 1957. Let's Go Over the Hill, *Phot. Eng.*, Vol. 23, pp. 909-920.
- Szangolies, K., and W. Kunze, 1979. Topomat—a New Fully Automatic Restitution System from Jena, *Kompendium Photogrammetrie*, Vol. XIII, Leipzig, pp. 100-120.
- Wrobel, B., 1978. Geometrische Aspekte der Korrelationssteuerung, Symp. über den Einsatz dig. Kompon. i.d. Photogrammetrie, IPI Hannover.